

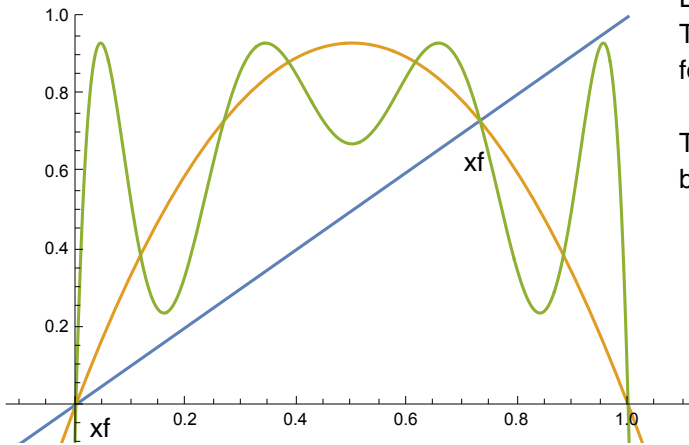
In[35]:=

```

f[x_, r_] := r * x * (1 - x)
f3[x_, r_] := f[f[f[x, r], r], r]
Plot[{x, f[x, 1 + Sqrt[8] - 0.1], f3[x, 1 + Sqrt[8] - 0.1]},
{x, -0.1, 1.1}, PlotRange -> {-0.1, 1}]

```

Out[37]=



Logistic map for $r < P3$ window.

The original fix points xf exist but became unstable for much lower r , ie, at r_{PD} .

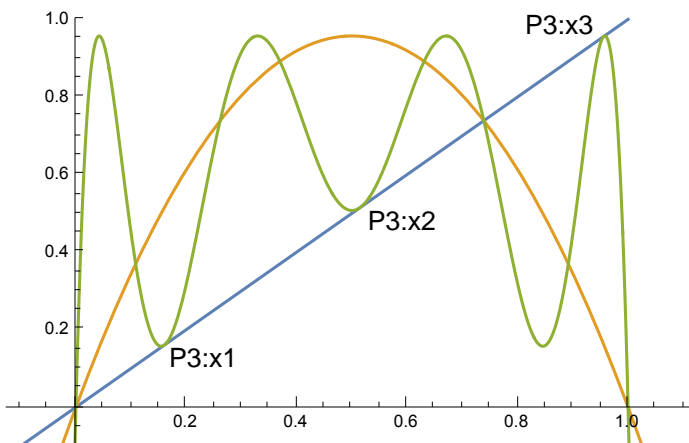
The $f3$ map has those same fixed points (unstable) but not yet any others.

```

In[33]:= Plot[{x, f[x, 1 + Sqrt[8]], f3[x, 1 + Sqrt[8]]}, {x, -0.1, 1.1}, PlotRange -> {-0.1, 1}]

```

Out[33]=



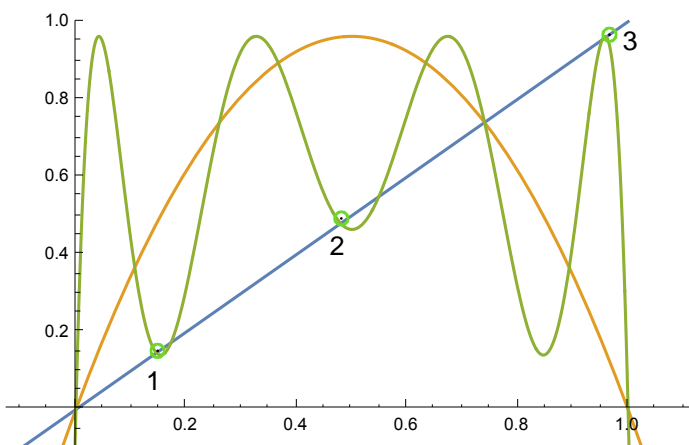
At $r = 1 + \sqrt{8}$ the $f3$ map is undergoing a saddle-node bifurcations to generate a $P3$ orbit.

```

In[41]:= Plot[{x, f[x, 1 + Sqrt[8] + 0.02], f3[x, 1 + Sqrt[8] + 0.02]},
{x, -0.1, 1.1}, PlotRange -> {-0.1, 1}]

```

Out[41]=



The 3 labeled points are the nodes of the $f3$ map corresponding to the $P3$ orbit of f . The unlabeled three points are saddles (unstable); note the local slope is greater than 1 at each of these points.